

Welcome to the homework page **test1**. If this isn't you then please go back to the [homework login page](#).

You may log out and return later if you wish without losing any saved data. You will have **TEN** attempts for each assigned problem. Every unsuccessful attempt will lower that part of the problem's value by 5%.

For example, if you get it right on the first try, then you will receive 100% for that problem. If you are twice incorrect and submit the correct on the third try, then you will receive a 90% for that part of the problem. You will not receive any points for that part of the problem after 10 attempts.

You do not have to answer all the problems during a single session or in any particular order. To answer a problem simply type the numerical value in the box provided, check the box to the right of the part(s) you want to answer, and then click the submit button. You can freely log in and out of the homework page without losing any submitted information so feel free to take breaks if necessary.

LET'S BEGIN! $\oint \vec{E} \cdot d\vec{A} = \frac{Q_{ENC}}{\epsilon_0}$ $4\pi R^2 E(R) = \frac{Q_{ENC}(R)}{\epsilon_0}$ $Q_{ENC} = \frac{4\pi r^3 \rho}{3}$

a) r_1 INSIDE SPHERE! $\Rightarrow E(r_1) = \frac{r_1 \rho}{3\epsilon_0} = \frac{(0.52)(3.40 \times 10^{-11})}{3(8.85 \times 10^{-12})}$

Problem #1

A sphere of radius $R = 79.0\text{cm}$ is an insulator into which has been placed a uniform (volumetric) charge density of $\rho = 3.40 \times 10^{-11}\text{C/m}^3$. Determine the electric field at the radial distance (a) $r_1 = 52.0\text{cm}$ and (b) $r_2 = 90.0\text{cm}$ from the center of the sphere.

(Take the permittivity of free space to be $\epsilon_0 = 8.854 \times 10^{-12}\text{F/m}$.)

(a) N/C $\hat{r}$ ☒ Answer part (a)

(b) N/C $\hat{r}$ ☒ Answer part (b)

Submit

Attempted part (a) 0 times and part (b) 0 times.

There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

$\Rightarrow$ FOR (b) $E(r_2) = \frac{Q_{ENC}}{4\pi\epsilon_0 r_2^2} = \frac{k Q_{TOT}}{r_2^2}$

$= \frac{(9 \times 10^9)(7.02 \times 10^{-11})}{(0.90)^2}$

So

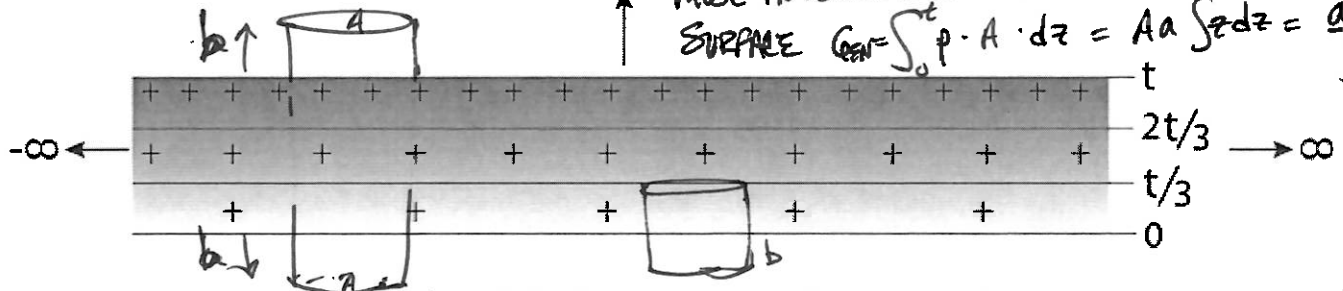
$E(r_2) = 0.78$

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Problem #2

SYMMETRY OF $\vec{E}$
SLAB: THEN

IDEA HERE IS TO DO THIS IN TWO STEPS. FIRST USE
FOR A GAUSSIAN CYLINDER $\rightarrow$ BOTH ENDS OUTSIDE THE CHARGE
 $\oint \vec{E} \cdot d\vec{A} = 2A\vec{E}(b) = \frac{Q_{ENC}}{\epsilon_0}$ TO FIND Q_{ENC} ONE
MUST INTEGRATE THE CHARGE DENSITY OF THE GAUSSIAN
SURFACE $Q_{ENC} = \int \rho \cdot A \cdot dz = Aa \int_0^t z dz = \frac{aAt^2}{2}$



The graphic depicts a (infinite) slab of thickness $t = 75.0\text{cm}$ having a location-dependent (volumetric) charge density of $\rho = a \cdot z$ the slab extent along the z -axis is 0 to t and the coefficient ' a ' is measured as $a = 6.30 \times 10^{-10}\text{C/m}^4$. For the infinite slab, the z -component of the electric field is the only nonzero component, and we take the vertical axis to be the z -axis. Find the electric field (a) below the slab, (b) at $t/3$, (c) at $2t/3$, and (d) above the slab.

So $Q_{ENC} = \frac{aAt^2}{2} = \frac{(6.3 \times 10^{-10})(0.75)^2}{2} A$
 $= 1.77 \times 10^{-10} A$

$\Rightarrow 2A\vec{E}(b) = \frac{1.77 \times 10^{-10} A}{\epsilon_0}$

$\vec{E}(b) = 10.01 \text{ N/C}$, INDEP OF b
SAME ANS. FOR (a) & (d)

(a) N/C $\hat{z}$ ☒ Answer part (a)

(b) N/C $\hat{z}$ ☒ Answer part (b)

(c) N/C $\hat{z}$ ☐ Answer part (c)

(d) N/C $\hat{z}$ ☒ Answer part (d)

POINTS DOWN
 $\rightarrow$ SIGN

Submit

FOR PARTS b, c NEED A DIFFERENT GAUSSIAN SURFACE, SHOWN ABOVE. IT
ENDS @ $t/3$, BUT STICKS OUTSIDE. THEN $\oint \vec{E} \cdot d\vec{A} = A\vec{E}(t/3) + A\vec{E}(b)$
 $\oint \vec{E} \cdot d\vec{A} = \frac{Q_{ENC}}{\epsilon_0}$
 $\Rightarrow A\vec{E}(t/3) + A\vec{E}(b) = 2.21A$
 $\vec{E}(t/3) = -7.79$, SO POINTS DOWN AS EXPECTED

Attempted part (a) 0 times, part (b) 0 times, part (c) 0 times, and part (d) 0 times.

There have been no attempts to answer part (a)

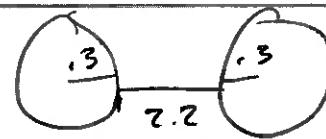
There have been no attempts to answer part (b)

There have been no attempts to answer part (c)

There have been no attempts to answer part (d)

SIMILARLY FOR (C), $Q_{ENC} = \frac{4aAt^2}{18}$
 $\vec{E}(2t/3) = -1.17$

Problem #3



Two spheres are metal and have the same radius $R = 30.0\text{cm}$. They can be connected by a wire (length $L = 2.20\text{m}$), but initially the wire is not connected when a charge of

$Q = 48.0 \mu\text{C}$ is placed on one of the spheres. Then, the wire is then connected. (a) What is the charge in the second sphere a short while after the wire is connected? (b) Assuming that the charges are approximately uniformly distributed over the spheres after the wire is reconnected, then what is the magnitude of the tension in the wire?

(a) μC ☒ Answer part (a)

(b) N ☒ Answer part (b)

Submit

d IS DISTANCE BETWEEN CENTERS!!

a) SPHERE IDENTICAL, EXPECT EQUAL AMOUNT OF CHARGE ON EACH, BY SYMMETRY.
 b) $F = \frac{kQ_1Q_2}{d^2} = \frac{(9 \times 10^9)(24 \times 10^{-6})^2}{(2.2 + .6)^2}$

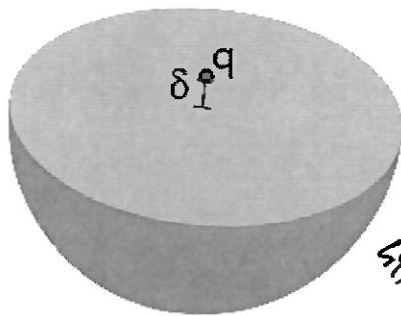
$F = 0.661 \text{ N}$

Attempted part (a) 0 times and part (b) 0 times.

There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

Problem #4



a) CONSIDER A VERY FAT "TUNA CAN" AROUND q , ONE FACE OF WHICH IS THE CIRCLE SHOWN
 $\oint \vec{E} \cdot d\vec{A} = q/\epsilon_0$
 SO SINCE, YOU CAN NEGLECT THE EDGE IS SAME TOP & BOTTOM. (EDGE IS ONE FACE.)
 $\Rightarrow \oint \vec{E} \cdot d\vec{A} = q/2\epsilon_0$

SP b) ANS. 15-5.93

- SINCE ITS GOING INTO THE SURFACE

A hemispherical volume has a point charge, $q = 1.05 \text{ nC}$, placed a small distance δ above the center of the flat surface, where $\delta \rightarrow 0$. (a) What is the flux through the curved surface of the hemisphere? (b) What is the flux through the flat surface? (Assume that field lines leaving the hemisphere give positive flux and lines entering the hemisphere give negative flux.)

(a) Nm^2/C ☐ Answer part (a)

(b) Nm^2/C ☒ Answer part (b)

Submit

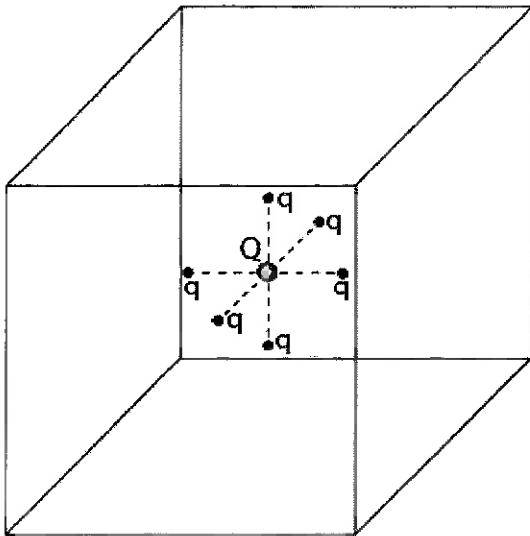
Attempted part (a) 0 times and part (b) 0 times.

FOR (a) AGAIN ITS 1/2 FLUX FROM CHARGE, AS IN (b) ✓
 AND ANOTHER WAY; THERES NO CHARGE IN HEMISPHERICAL VOLUME SO
 $Q_{ENC}/\epsilon_0 = 0 = \oint \vec{E} \cdot d\vec{A} = \oint_{\text{FLAT CIRCLE}} \vec{E} \cdot d\vec{A} + \oint_{\text{HEMISPHERE}} \vec{E} \cdot d\vec{A}$
 SO MUST BE EQUAL & OPPOSITE SIGN

There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

Problem #5



By Sym. All faces same.

$$\oint \vec{E} \cdot d\vec{A} = 6 \int_{\text{FACE}} \vec{E} \cdot d\vec{A}$$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{ENC}}}{\epsilon_0} = \frac{(-5.2 + 6(1.3)) \text{ nC}}{\epsilon_0}$$

$$= 293.8$$

A cube of sidelength $L = 1.10\text{m}$ encloses a charge $Q = -5.20\text{nC}$ that is surrounded by six charges of $q = 1.30\text{nC}$ that are symmetrically placed along the axial dimensions of the cube. What is the electric flux through the right side of the cube?

48.96

Nm²/C



Answer the question

Submit

So $\oint \vec{E} \cdot d\vec{A} = \frac{293.8}{6}$

ONE FACE

48.96

Attempted the problem 0 times.

There have been no attempts to answer the problem

Problem #6

THIS IS SCHEMATICALLY JUST LIKE THE UNIFORMLY CHARGED SPHERE, PROBLEM #1 (a), (b) ARE INSIDE (c), (d) ARE OUTSIDE. $R = 0.7$ TAKE AS GAUSSIAN SURFACES CYLINDERS, SINCE $\vec{E}$ POINTS OUT!

A cylinder (straight and assumed to be infinitely long) is of radius $R = 70.0\text{cm}$.

Throughout its volume is placed a uniform charge density $\rho = 0.125\text{nC/m}^3$. What is the electric field at (a) $r_1 = 41.0\text{cm}$, (b) $r_2 = 52.0\text{cm}$, (c) $r_3 = 81.0\text{cm}$, and (d) $r_4 = 94.0\text{cm}$? Use cylindrical coordinates (r, ϕ, z) .

(a)

2.896

N/C $\hat{r}$



Answer part (a)

BUT $Q_{\text{ENC}} = \rho \cdot V_{\text{cyl}}$

$$= \rho \cdot \pi r^2 h$$

THEN $\oint \vec{E} \cdot d\vec{A} = 2\pi r h E(r)$

$$= Q_{\text{ENC}} / \epsilon_0$$

SO $2\pi r h E(r) = \frac{\rho \pi r^2 h}{\epsilon_0}$

FOR $r < R$: (a), (b)

So for (a), (b)

$$E(r) = \frac{\rho r}{2\epsilon_0}$$

FOR (c), (d)

$$r > R \quad E(r) = \frac{\rho R^2}{2\epsilon_0 r}$$

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- (b) N/C $\hat{r}$ ☒ Answer part (b)
- (c) N/C $\hat{r}$ ☒ Answer part (c)
- (d) N/C $\hat{r}$ ☒ Answer part (d)

Submit

Attempted part (a) 0 times, part (b) 0 times, part (c) 1 times, and part (d) 0 times.

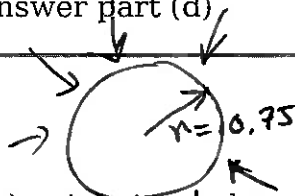
There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

Part (c) has been answered correctly

There have been no attempts to answer part (d)

Problem #7



An electric field (assumed uniform) points inward towards a spherical surface of $r = 75.0\text{cm}$, which encloses a charge. The magnitude of the electric field at any location on the surface is measured to be $|\mathbf{E}| = 82.5\text{N/C}$. if no other charges are present outside sphere, then what is the net charge inside the closed spherical surface?

nC

☒ Answer the question

Submit

Attempted the problem 0 times.

There have been no attempts to answer the problem

So Plug in $r = 0.75\text{m}$

$$(a) \ E(r) = \frac{Q}{4\pi\epsilon_0 r^2} = \frac{(6.125 \times 10^{-9})(0.41)}{2(8.85 \times 10^{-12})} = 2.8955$$

$$(b) \ E(r) = \frac{(0.125 \times 10^{-9})(0.52)}{2(8.85 \times 10^{-12})} = 3.67$$

$$(c) \ E(r) = \frac{Qr^2}{2\epsilon_0} = \frac{(0.125 \times 10^{-9})(.7)^2}{2(8.85 \times 10^{-12})(0.81)} = 4.27$$

$$(d) \ E(r) = \frac{(0.125 \times 10^{-9})(.7)^2}{2(8.85 \times 10^{-12})(0.94)} = 3.681$$

Problem #8

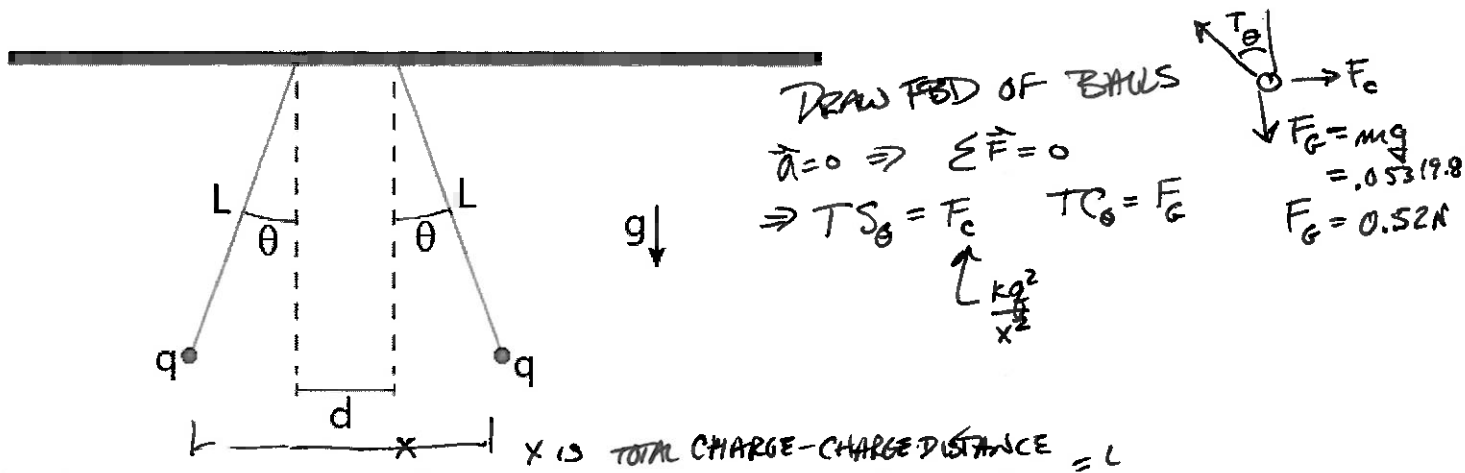
NOTE - SINCE IT'S POINTING INWARD ($d\mathbf{A}$ POINTS OUT!)

BY GAUSS: $\oint \mathbf{E} \cdot d\mathbf{A} = Q_{\text{ENC}}/\epsilon_0 \Rightarrow Q_{\text{ENC}} = -583\epsilon_0$

$$\oint \mathbf{E} \cdot d\mathbf{A} = -4\pi r^2 |\mathbf{E}| = -583 \frac{\text{Nm}^2}{\text{C}}$$

$$Q_{\text{ENC}} = -5.161 \times 10^{-9} \text{C}$$

$$= -5.161 \text{ nC}$$



Little spheres (shown hanging from insulating threads of length 11.0 cm) have the same mass (0.0530 kg) and a charge is placed on the pair so that it is evenly distributed between them. They are hung a distance $d = 7.20 \text{ cm}$ from each other (as shown) on the ceiling. Compute the magnitude of the charge on a single sphere if they hang at an angle of (a) $\theta = 10.0^\circ$ and (b) $\theta = 16.0^\circ$?

(a) μC ☒ Answer part (a)

(b) μC ☒ Answer part (b)

Submit

Attempted part (a) 0 times and part (b) 0 times.

There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

NOTE For Part (a) $\theta = 10^\circ$, $x = d + 2L \sin \theta = 0.072 + 2(0.11) \sin 10^\circ = 0.0911$

$$T = F_g / \cos \theta = 0.528 \text{ N} \quad \text{THEN} \quad T \sin \theta = \frac{k q^2}{x^2} \quad q^2 = \frac{x^2 T \sin \theta}{k}$$

a) $q^2 = \frac{(0.0911)^2 (0.528) \sin 10^\circ}{9 \times 10^9} = 8.45 \times 10^{-14} \Rightarrow q = 2.91 \times 10^{-7} \text{ C}$

b) $\theta = 16^\circ$ $x = d + 2L \sin 16^\circ = 0.133$

$$T = F_g / \cos 16^\circ = 0.541$$

$$q^2 = \frac{x^2 T \sin 16^\circ}{k} = 2.931 \times 10^{-13}$$

$$\Rightarrow q = 5.41 \times 10^{-7} \text{ C}$$