

= KEY =

HW #3

Welcome to the homework page **test1**. If this isn't you then please go back to the homework login page.

You may log out and return later if you wish without losing any saved data. You will have **TEN** attempts for each assigned problem. Every unsuccessful attempt will lower that part of the problem's value by 5%.

For example, if you get it right on the first try, then you will receive 100% for that problem. If you are twice incorrect and submit the correct on the third try, then you will receive a 90% for that part of the problem. You will not receive any points for that part of the problem after 10 attempts.

You do not have to answer all the problems during a single session or in any particular order. To answer a problem simply type the numerical value in the box provided, check the box to the right of the part(s) you want to answer, and then click the submit button. You can freely log in and out of the homework page without losing any submitted information so feel free to take breaks if necessary.

LET'S BEGIN!

Problem #1

$$E = \frac{kQ}{x^2}$$

$$V = \frac{kQ}{x}$$

A evenly charged sphere causes the magnitude of the electric field somewhere outside to be 475V/m. At that same place the electric potential is 3.10kV (note 'kV' means kilovolts). (a) How far is this place from the center of the object? (b) What is the magnitude of the charge?

(a) m ☒ Answer part (a)

(b) μC ☒ Answer part (b)

Submit

Attempted part (a) 0 times and part (b) 0 times.

There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

(a) $\Rightarrow$ Solve for x.

Note $\frac{V}{E} = x = \frac{3100}{475} = 6.53$

(b) Now that we know x, we can go back & solve for Q.

$$V = \frac{kQ}{x} \Rightarrow Q = \frac{Vx}{k} = \frac{(3100)(6.53)}{9 \times 10^9}$$

$$\Rightarrow Q = 2.25 \times 10^{-6} \text{ C}$$

$$V = -\int \vec{E} \cdot d\vec{r}$$

Problem #2

$$\Rightarrow \vec{E} = -\vec{\nabla} V$$

$$E_x = -\frac{dV}{dx} = (-x - 0.75x^2)(-1)$$

The electric potential along the x-direction due to an unevenly charged structure has, as a function of distance 'x', the potential $V(x) = 1.00 \text{ V} - (0.500 \text{ V/m}^2)x^2 - (0.250 \text{ V/m}^3)x^3$. Compute the electric field at x= (a) 25.0cm, and (b) x= 55.0cm, (c) 73.0cm, and (d) 1.05m?

(a) N/C ☒ Answer part (a)

$$\begin{aligned} a) V(0.25) &= +0.25 + 0.75(0.25)^2 \\ &= +0.297 \end{aligned}$$

(b) N/C ☐ Answer part (b)

(c) N/C ☐ Answer part (c)

REST SAME ... JUST Plug
IN $x = \dots$

(d) N/C ☐ Answer part (d)

$$\text{INTO } E_x = x + 0.75x^2$$

Submit

Attempted part (a) 0 times, part (b) 0 times, part (c) 0 times, and part (d) 0 times.

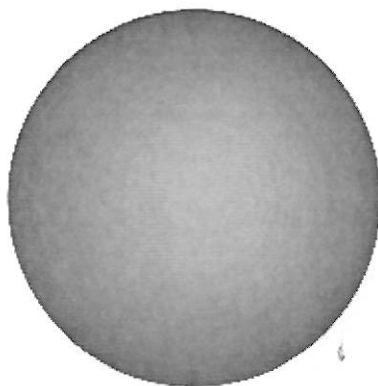
There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

There have been no attempts to answer part (c)

There have been no attempts to answer part (d)

Problem #3



a) TO GET TO ∞ , $V(\infty) = 0$ SO SINCE ENERGY IS CONSERVED $U_{\text{SURFACE}} = U_{\infty}$

$$\frac{1}{2}mv^2 + \frac{kQq}{R} = 0$$

IF JUST MAKES IT OUT FAR AWAY W/ ESSENTIALLY NO VELOCITY.

$$\frac{1}{2}mv^2 = -\frac{kQq}{R}$$

$$= \frac{-(9 \times 10^9)(-355 \times 10^{-6})(4.2 \times 10^{-9})}{(2.3)^2}$$

$$\frac{1}{2}(0.011)v^2 = 0.0025 \Rightarrow v = 0.679 \text{ m/s}$$

A spherical object with radius $R = 2.30\text{cm}$ and net charge $Q = -355\mu\text{C}$ throws out from its surface a charged (positive) chunk of mass $m = 11.0\text{g}$ and charge $q = 4.20\text{nC}$. (a) What must be the initial velocity of ejection for the chunk to escape the large object's Coulomb potential (escape velocity...that is, the minimum initial velocity at the surface for the chunk to go infinitely far away). (b) What was the kinetic energy at the surface when traveling at this escape velocity?

(a) m/s ☒ Answer part (a)

b) $\frac{1}{2}mv^2$, BUT THAT - OF P.F.
 $= 0.0025 \text{ J}$

(b) J ☒ Answer part (b)

Submit

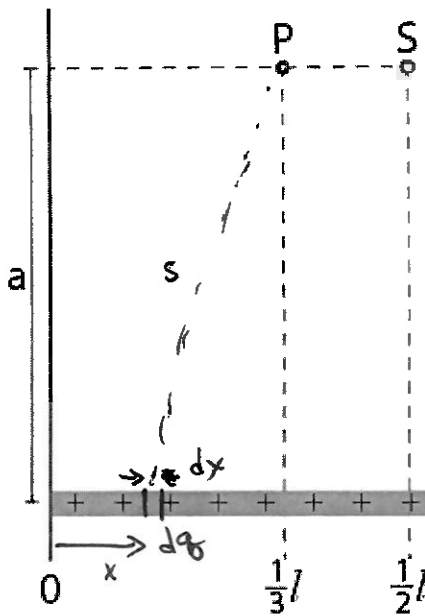
Attempted part (a) 0 times and part (b) 0 times.

There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

Problem #4

CHOOSE A CO-ORD ALONG CHARGE.



$$dq = \lambda dx \quad \text{where } \lambda = \frac{Q}{l} = 5.92 \times 10^{-9} \frac{\text{C}}{\text{m}}$$

CHARGE PER UNIT LENGTH

$$V = \int dV = \int \frac{k dq}{r} = k \lambda \int_0^l \frac{dx}{\sqrt{(x-x_0)^2 + y_0^2}}$$

$y_0 = a$, BUT (a) For P, $x_0 = l/3$ For (b) S, $x_0 = l/2$ SO
NOTE IS GENERAL, $u = x - x_0$ $du = dx$ LET $u = y_0 \sinh w$
 $du = y_0 \cosh w dw$ $1 + \sinh^2 w = \cosh^2 w$

$$\int \frac{du}{\sqrt{u^2 + y_0^2}} = \int \frac{y_0 \cosh w dw}{y_0 \cosh w} = w \quad \text{so } \frac{u}{y_0} = \sinh w = \frac{e^w - e^{-w}}{2}$$

SO NOTE ~~$\frac{u}{y_0} = \sinh w$~~ $\frac{u}{y_0} = \sinh w = \frac{e^w - e^{-w}}{2}$
 $\Rightarrow e^{2w} - 2\left(\frac{u}{y_0}\right)e^w - 1 = 0 \Rightarrow$

QUADRATIC FORMULA: $e^w = \frac{u}{y_0} \pm \sqrt{\left(\frac{u}{y_0}\right)^2 + 1}$ - SIGN HAS PROBLEM

A rod of length $\ell = 1.20\text{m}$ and uniform charge $Q = 7.10\text{nC}$ is positioned along the x-axis. As depicted in the above diagram, two points are located a distance $a = 1.10\text{m}$ away from the rod in the y-direction. Point P is located a distance of $\ell/3$ from the end of the rod in the x-direction and point S is located a distance of $\ell/2$ from the end of the rod in the x-direction. Calculate the electric potential at (a) point P and (b) point S.

(a) V ☒ Answer part (a)

(b) V ☒ Answer part (b)

Submit

Attempted part (a) 0 times and part (b) 0 times.

There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

$$\int \frac{du}{\sqrt{u^2 + y_0^2}} = \ln\left(\frac{u}{y_0} + \sqrt{\left(\frac{u}{y_0}\right)^2 + 1}\right) \quad \text{SO}$$

$$a) V(P) = k \lambda \ln\left(\frac{x-x_0}{a} + \sqrt{\left(\frac{x-x_0}{a}\right)^2 + 1}\right) \Big|_0^l$$

where $x_0 = l/3 = 0.4$ $a = 1.1$

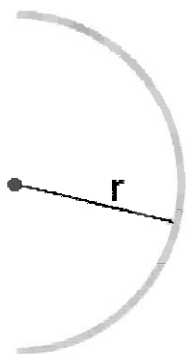
$$V(P) = (9 \times 10^9)(5.92 \times 10^{-9}) \left[\ln\left(\frac{.8}{1.1} + \sqrt{\left(\frac{.8}{1.1}\right)^2 + 1}\right) - \ln\left(\frac{-.4}{1.1} + \sqrt{\left(\frac{-.4}{1.1}\right)^2 + 1}\right) \right]$$

$$V(P) = 53.3(1.031)$$

$$= 54.93 \text{ VOLTS}$$

Problem #5

$$b) V(S) = 53.3(1.043) = 55.6 \text{ VOLTS}$$



$$V = \sum V_i = \frac{k}{r} \sum dq = \frac{kQ}{r}$$

$$V = \frac{(9 \times 10^9)(-1.7 \times 10^{-9})}{0.0414}$$

$$V = -369.7 \text{ volts}$$

$$= \pi r$$

$$r = 0.0414 \text{ m}$$

A uniformly charged insulating rod of length = 13.0cm is bent into the shape of a semicircle as shown in the above diagram. The rod has a total charge of $Q = -1.70 \text{ nC}$. What is the potential a distance r away from all points in the rod?

-369.7

V



Answer the question

Submit

Attempted the problem 0 times.

There have been no attempts to answer the problem

(b) INSIDE SPHERE $\vec{E} = 0 \Rightarrow$
 $V \text{ const.} = \frac{kQ}{r_0} = \frac{(9 \times 10^9)(2.3 \times 10^{-9})}{0.56}$
 $= 36.96 \text{ volts}$

Problem #6

A conducting sphere has a radius of $R = 56.0 \text{ cm}$ and a total charge of $Q = 2.30 \text{ nC}$. For a radial distance of $r_1 = 26.0 \text{ cm}$, calculate (a) the electric potential and (b) the magnitude of the electric field. For a radial distance of $r_2 = 81.0 \text{ cm}$, calculate (c) the electric potential and (d) the magnitude of the electric field.

(a) 36.96 V



Answer part (a)

(b) 0 V/m $\hat{r}$



Answer part (b)

(c) 25.56 V



Answer part (c)

(d) 31.55 V/m $\hat{r}$



Answer part (d)

Submit

(b) OUTSIDE SPHERE
 $V = \frac{kQ}{r} = \frac{(9 \times 10^9)(2.3 \times 10^{-9})}{0.81}$
 $= 25.56 \text{ V}$

d) OUTSIDE SPHERE $E = \frac{kQ}{r^2}$
 $E = \frac{(9 \times 10^9)(2.3 \times 10^{-9})}{(0.81)^2}$
 $= 31.55 \text{ V/m}$

Attempted part (a) 0 times, part (b) 0 times, part (c) 0 times, and part (d) 0 times.

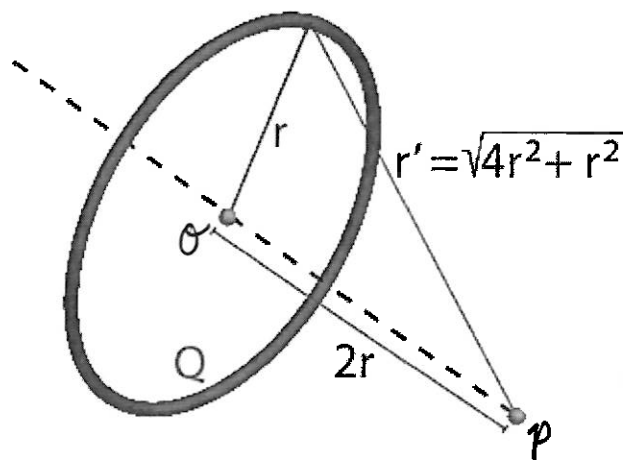
There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

There have been no attempts to answer part (c)

There have been no attempts to answer part (d)

Problem #7



$$V = \sum V_n = k \sum \frac{q_n}{r_n}$$

$$\text{For } O \quad V(O) = \frac{k}{r} \sum q_n = \frac{kQ}{r}$$

SINCE ALL q_n ARE SAME DISTANCE r FROM O .

$$V(O) = \frac{(9 \times 10^9)(1.4 \times 10^{-9})}{0.76} = 16.6 \text{ VOLTS}$$

$$\text{But @ } P. \quad V(P) = k \sum \frac{q_n}{r_n} = \frac{k}{r'} \sum q = \frac{kQ}{r'}$$

$$\text{w/ } r' = \sqrt{4r^2 + r^2} = \sqrt{5}r = 1.7 \text{ m} \quad \text{so } \Rightarrow \quad V(P) = \frac{(9 \times 10^9)(1.4 \times 10^{-9})}{1.7} = 7.4 \text{ V}$$

A ring of radius $r = 76.0\text{cm}$ has a total charge of $Q = 1.40\text{nC}$ spread uniformly over its perimeter. Calculate the magnitude of the difference in electric potential between the point at the center of the ring and a point that is a distance of $2r$ away from the ring and lying on the ring's z-axis.

9.19

v



Answer the question

Submit

$$\text{so } \Delta V = |V(O) - V(P)|$$

$$= 9.19 \text{ VOLTS}$$

Attempted the problem 0 times.

There have been no attempts to answer the problem

Problem #8

$$= \frac{kQ}{r_0}$$

The electric potential inside a conducting sphere is 185V , and a distance $d =$

$$V = V_0 + 0.24$$

24.0cm from the surface of the sphere, the potential is 135V. Calculate (a) the radius of the sphere and (b) the charge on the sphere.

(a) cm ☒ Answer part (a)

(b) nC ☒ Answer part (b)

Submit

Attempted part (a) 0 times and part (b) 0 times.

There have been no attempts to answer part (a)

There have been no attempts to answer part (b)

SO 1ST SENTENCE IS

$$\frac{kQ}{r_0} = 185$$

2ND SENTENCE IS

$$\frac{kQ}{r_0 + 0.24} = 135$$

TAKE ONE EQUATION & DIVIDE IT BY THE OTHER! KQ'S DROP OUT

$$\frac{r_0 + 0.24}{r_0} = \frac{185}{135}$$

$$1 + \frac{0.24}{r_0} = \frac{185}{135}$$

$$\Rightarrow r_0 = 0.648$$

SO PROG THAT BACK INTO FIND Q.

$$\frac{(9 \times 10^9)Q}{0.648} = 185 \Rightarrow Q = 13.32 \text{ nC}$$